

```

1 restart;maple_mode(1);cas_setup(0,0,0,1,0,1e-10,10,[1,50,0,25],0,0,0);#radians,pas de cmplx, pas de Sqrt
( [], Warning: some commands like subs might change arguments order , 0, 0, 0, 1, 0, 1e-10, 10, [ 1 5
2
3 Prog Edit Add      |      |      |      |      |      |      |      |      |      |      |
  |      |      |      |      |      |      |      |      |      |      |      |      |
  |      |      |      |      |      |      |      |      |      |      |      |      |
monpolyfaddeev:= proc (A)
local a,n,B,P;
n:=dim(A)[1];a:=1:B:=identity(n);P:=a;
for i from n-1 to 0 by -1 do
B:=normal(B*A);
a:=trace(B)/(i-n);
P:=op(P),a;B:=B+a*identity(n) od;
P;
end proc :

// Warning: i declared as global variable(s)
// End defining monpolyfaddeev

Done

4 n:=30;A:=matrix(n,n,(i,j)->rand(21)-10);
// Success
( 30, Done )

5 normal(poly2symb(monpolyfaddeev(A),x));
Evaluation time: 0.94

x30 + (-7) · x29 + (-387) · x28 + (-8113) · x27 + 360369 · x26 + (-1130723) · x25 + (-8725679) · x24 + 4428175555 · x23
+ 1004212188740741 · x19 + 32796413776225308 · x18 + (-7525306724112494109) · x17 + 3943048108018032086 · x16
+ (-1311391537081447567579255) · x13 + 75450981687489027655392125 · x12 + (-125523283147439215831316) · x11
+ (-146815700499140223810594848674) · x9 + 6859146575926265288604929987028 · x8 + 24362820480375805 · x7
+ (-29317463714002218897042238598557291) · x5 + 989403999101509545788744924015897910 · x4 + (-16662) · x3
+ (-29517956559930572984260991577837663929) · x2 + 649251732900074175864953663626279262822 · x + 8

6 charpoly(A)-monpolyfaddeev(A);
Evaluation time: 1.11
0

7 time(monpolyfaddeev(A));
Evaluation time: 0.96
0.96

8 time(charpoly(A));
0.16

9 coeff(3*x^4+2*x^3+y^3,x,3);
2

10 A:=matrix(3,4,2);matrix(op(dim(A)));
( 2 2 2 2 | 0 0 0 0
  2 2 2 2 | 0 0 0 0
  2 2 2 2 | 0 0 0 0 )
11

```

```
12 Prog Edit Add      |      |      |      |      |      |      |
| cf:=proc(P,k)      |
| local i,j;         |
| matrix(op(dim(P)),(i,j)->coeff(P[i,j],x,k));
| end_proc ;
|
| // Warning: x declared as global variable(s)
| // End defining cf
|
| proc(P,k)
| local i,j;
| matrix(op(dim(P)),(i,j)->coeff(P[i,j],x,k));
|
| end;
```

```
13 P:=matrix(3,3,(i,j)->add(rand(7)*x^i,l=0..4));
| // Warning: x l declared as global variable(s)
|
| 
$$\begin{bmatrix} 5+3 \cdot x+x^3+5 \cdot x^4 & 2+6 \cdot x+6 \cdot x^2+2 \cdot x^3+2 \cdot x^4 & 5+6 \cdot x+5 \cdot x^2+x^3+x^4 \\ 3+2 \cdot x^2+3 \cdot x^3+6 \cdot x^4 & 3+4 \cdot x+x^2+x^3+3 \cdot x^4 & 6+5 \cdot x+2 \cdot x^2+x^3+3 \cdot x^4 \\ 6+5 \cdot x+2 \cdot x^2+4 \cdot x^3+4 \cdot x^4 & 6 \cdot x+5 \cdot x^2+x^3+2 \cdot x^4 & 6+5 \cdot x^2+3 \cdot x^3+2 \cdot x^4 \end{bmatrix}$$

```

```
14 A:=matrix(3,3,(i,j)->a[i,j]);
| // Warning: a declared as global variable(s)
|
| 
$$\begin{bmatrix} a[[ 1, 1 ]] & a[[ 1, 2 ]] & a[[ 1, 3 ]] \\ a[[ 2, 1 ]] & a[[ 2, 2 ]] & a[[ 2, 3 ]] \\ a[[ 3, 1 ]] & a[[ 3, 2 ]] & a[[ 3, 3 ]] \end{bmatrix}$$

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```
15 cf(P,4);
|
| 
$$\begin{bmatrix} 5 & 2 & 1 \\ 6 & 3 & 3 \\ 4 & 2 & 2 \end{bmatrix}$$

```

```
16 R:=P;k:=4;Q:=0;
|
| 
$$\left( \begin{bmatrix} 5+3 \cdot x+x^3+5 \cdot x^4 & 2+6 \cdot x+6 \cdot x^2+2 \cdot x^3+2 \cdot x^4 & 5+6 \cdot x+5 \cdot x^2+x^3+x^4 \\ 3+2 \cdot x^2+3 \cdot x^3+6 \cdot x^4 & 3+4 \cdot x+x^2+x^3+3 \cdot x^4 & 6+5 \cdot x+2 \cdot x^2+x^3+3 \cdot x^4 \\ 6+5 \cdot x+2 \cdot x^2+4 \cdot x^3+4 \cdot x^4 & 6 \cdot x+5 \cdot x^2+x^3+2 \cdot x^4 & 6+5 \cdot x^2+3 \cdot x^3+2 \cdot x^4 \end{bmatrix}, 4, 0 \right)$$

```

```
17 R:=normal(R-cf(R,k)*x^(k-1)*(x*identity(3)-A));Q:=cf(R,k)*x^(k-1)+Q;k:=k-1;
|
| 
$$\begin{bmatrix} 5 \cdot x^3 \cdot (a[[ 1, 1 ]])+ & 5 \cdot x^3 \cdot (a[[ 1, 2 ]])+ & 5 \cdot x^3 \cdot (a[[ 1, 3 ]])+ \\ 2 \cdot x^3 \cdot (a[[ 2, 1 ]])+ & 2 \cdot x^3 \cdot (a[[ 2, 2 ]])+ & 2 \cdot x^3 \cdot (a[[ 2, 3 ]])+ \\ x^3 \cdot (a[[ 3, 1 ]])+x^3+3 \cdot x+5 & x^3 \cdot (a[[ 3, 2 ]])+2 \cdot x^3+6 \cdot x^2+6 \cdot x+2 & x^3 \cdot (a[[ 3, 3 ]])+x^3+5 \\ 6 \cdot x^3 \cdot (a[[ 1, 1 ]])+ & 6 \cdot x^3 \cdot (a[[ 1, 2 ]])+ & 6 \cdot x^3 \cdot (a[[ 1, 3 ]])+ \\ 3 \cdot x^3 \cdot (a[[ 2, 1 ]])+ & 3 \cdot x^3 \cdot (a[[ 2, 2 ]])+ & 3 \cdot x^3 \cdot (a[[ 2, 3 ]])+ \\ 3 \cdot x^3 \cdot (a[[ 3, 1 ]])+3 \cdot x^3+2 \cdot x^2+3 & 3 \cdot x^3 \cdot (a[[ 3, 2 ]])+x^3+x^2+4 \cdot x+3 & 3 \cdot x^3 \cdot (a[[ 3, 3 ]])+x^3 \\ 4 \cdot x^3 \cdot (a[[ 1, 1 ]])+ & 4 \cdot x^3 \cdot (a[[ 1, 2 ]])+ & 4 \cdot x^3 \cdot (a[[ 1, 3 ]])+ \\ 2 \cdot x^3 \cdot (a[[ 2, 1 ]])+ & 2 \cdot x^3 \cdot (a[[ 2, 2 ]])+ & 2 \cdot x^3 \cdot (a[[ 2, 3 ]])+ \\ 2 \cdot x^3 \cdot (a[[ 3, 1 ]])+4 \cdot x^3+2 \cdot x^2+5 \cdot x+6 & 2 \cdot x^3 \cdot (a[[ 3, 2 ]])+x^3+5 \cdot x^2+6 \cdot x & 2 \cdot x^3 \cdot (a[[ 3, 3 ]])+3 \cdot \end{bmatrix}$$

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18 R:=normal(R-cf(R,k)*x^(k-1)*(x*identity(3)-A));Q:=cf(R,k)*x^(k-1)+Q;k:=k-1;

$$\begin{aligned} &5 \cdot x^2 \cdot (a[1, 1])^2 + 5 \cdot x^2 \cdot (a[1, 1]) \cdot (a[1, 2]) + 5 \cdot x^2 \cdot (a[1, 1]) \cdot (a[1, 3]) + \\ &2 \cdot x^2 \cdot (a[1, 1]) \cdot (a[2, 1]) + 2 \cdot x^2 \cdot (a[1, 2]) \cdot (a[2, 1]) + 5 \cdot x^2 \cdot (a[1, 1]) \cdot (a[2, 3]) + \\ &x^2 \cdot (a[1, 1]) \cdot (a[3, 1]) + 5 \cdot x^2 \cdot (a[1, 2]) \cdot (a[2, 2]) + 5 \cdot x^2 \cdot (a[1, 2]) \cdot (a[2, 3]) + \\ &x^2 \cdot (a[1, 1]) + x^2 \cdot (a[1, 2]) \cdot (a[3, 1]) + 2 \cdot x^2 \cdot (a[1, 3]) \cdot (a[3, 1]) + \\ &5 \cdot x^2 \cdot (a[1, 2]) \cdot (a[2, 1]) + x^2 \cdot (a[1, 2]) + x^2 \cdot (a[1, 3]) \cdot (a[3, 1]) + \\ &5 \cdot x^2 \cdot (a[1, 3]) \cdot (a[3, 1]) + 5 \cdot x^2 \cdot (a[1, 3]) \cdot (a[3, 2]) + 5 \cdot x^2 \cdot (a[1, 3]) \cdot (a[3, 3]) + \\ &2 \cdot x^2 \cdot (a[2, 1]) \cdot (a[2, 2]) + 2 \cdot x^2 \cdot (a[2, 2])^2 + x^2 \cdot (a[1, 3]) + \\ &x^2 \cdot (a[2, 1]) \cdot (a[3, 2]) + x^2 \cdot (a[2, 2]) \cdot (a[3, 2]) + 2 \cdot x^2 \cdot (a[2, 2]) \cdot (a[2, 3]) + \\ &2 \cdot x^2 \cdot (a[2, 1]) + 2 \cdot x^2 \cdot (a[2, 2]) + x^2 \cdot (a[2, 3]) \cdot (a[3, 2]) + \\ &2 \cdot x^2 \cdot (a[2, 3]) \cdot (a[3, 1]) + 2 \cdot x^2 \cdot (a[2, 3]) \cdot (a[3, 2]) + 2 \cdot x^2 \cdot (a[2, 3]) \cdot (a[3, 3]) + \\ &x^2 \cdot (a[3, 1]) \cdot (a[3, 3]) + x^2 \cdot (a[3, 2]) \cdot (a[3, 3]) + 2 \cdot x^2 \cdot (a[2, 3]) + \\ &x^2 \cdot (a[3, 1]) + 3 \cdot x + 5 \quad x^2 \cdot (a[3, 2]) + 6 \cdot x^2 + 6 \cdot x + 2 \quad x^2 \cdot (a[3, 3])^2 + x^2 \cdot (a[3, 3]) \end{aligned}$$

19 R:=normal(R-cf(R,k)*x^(k-1)*(x*identity(3)-A));Q:=cf(R,k)*x^(k-1)+Q;k:=k-1;

$$\begin{aligned} &2 \cdot x \cdot (a[1, 1]) \cdot (a[2, 1]) \cdot (a[2, 2]) + 5 \cdot x \cdot (a[1, 2]) \cdot (a[1, 3]) \cdot (a[3, 1]) + \\ &x \cdot (a[1, 1]) \cdot (a[2, 1]) \cdot (a[3, 2]) + 4 \cdot x \cdot (a[1, 2]) \cdot (a[2, 1]) \cdot (a[3, 2]) + \\ &2 \cdot x \cdot (a[1, 1]) \cdot (a[2, 1]) + x \cdot (a[1, 2]) \cdot (a[2, 1]) \cdot (a[3, 2]) + \\ &2 \cdot x \cdot (a[1, 1]) \cdot (a[2, 3]) \cdot (a[3, 1]) + 2 \cdot x \cdot (a[1, 2]) \cdot (a[2, 1]) + \\ &x \cdot (a[1, 1]) \cdot (a[3, 1]) \cdot (a[3, 3]) + 5 \cdot x \cdot (a[1, 2]) \cdot (a[2, 2])^2 + \\ &x \cdot (a[1, 1]) \cdot (a[3, 1]) + x \cdot (a[1, 2]) \cdot (a[2, 2]) \cdot (a[3, 1]) + \\ &x \cdot (a[1, 2]) \cdot (a[2, 2]) + 2 \cdot x \cdot (a[1, 2]) \cdot (a[2, 3]) \cdot (a[3, 1]) + \\ &x \cdot (a[1, 2]) \cdot (a[2, 3]) \cdot (a[3, 3]) + 5 \cdot x \cdot (a[1, 2]) \cdot (a[2, 3]) \cdot (a[3, 3]) + \\ &5 \cdot x \cdot (a[1, 2]) \cdot (a[2, 3]) \cdot (a[3, 1]) + x \cdot (a[1, 2]) \cdot (a[3, 1]) \cdot (a[3, 3]) + \\ &2 \cdot x \cdot (a[1, 3]) \cdot (a[2, 1]) \cdot (a[3, 1]) + 2 \cdot x \cdot (a[1, 3]) \cdot (a[2, 1]) \cdot (a[3, 2]) + \\ &5 \cdot x \cdot (a[1, 3]) \cdot (a[2, 1]) \cdot (a[3, 2]) + 5 \cdot x \cdot (a[1, 3]) \cdot (a[2, 2]) \cdot (a[3, 1]) + \\ &x \cdot (a[1, 3]) \cdot (a[3, 1])^2 + x \cdot (a[1, 3]) \cdot (a[3, 1]) \cdot (a[3, 2]) + \\ &5 \cdot x \cdot (a[1, 3]) \cdot (a[3, 1]) \cdot (a[3, 3]) + 5 \cdot x \cdot (a[1, 3]) \cdot (a[3, 2]) \cdot (a[3, 3]) + \\ &x \cdot (a[1, 3]) \cdot (a[3, 1]) + x \cdot (a[1, 3]) \cdot (a[3, 2]) \end{aligned}$$

20 R:=normal(R-cf(R,k)*x^(k-1)*(x*identity(3)-A));Q:=cf(R,k)*x^(k-1)+Q;k:=k-1;

$$\begin{aligned} &5 \cdot (a[1, 1])^4 + 5 \cdot (a[1, 1])^3 \cdot (a[1, 2]) + \\ &2 \cdot (a[1, 1])^3 \cdot (a[2, 1]) + 2 \cdot (a[1, 1])^2 \cdot (a[1, 2]) \cdot (a[2, 1]) + \\ &(a[1, 1])^3 \cdot (a[3, 1]) + (a[1, 1])^3 + 15 \cdot (a[1, 1])^2 \cdot (a[1, 2]) \cdot (a[2, 1]) + \\ &15 \cdot (a[1, 1])^2 \cdot (a[1, 3]) \cdot (a[3, 1]) + (a[1, 1])^2 \cdot (a[1, 2]) \cdot (a[2, 2]) + \\ &(a[1, 1])^2 \cdot (a[2, 1]) \cdot (a[3, 2]) + 2 \cdot (a[1, 1])^2 \cdot (a[2, 1]) + \\ &2 \cdot (a[1, 1])^2 \cdot (a[2, 3]) \cdot (a[3, 1]) + (a[1, 1])^2 \cdot (a[3, 1]) \cdot (a[3, 3]) + \\ &(a[1, 1])^2 \cdot (a[3, 1]) + 4 \cdot (a[1, 1]) \cdot (a[1, 2]) \cdot (a[2, 1])^2 + \\ &10 \cdot (a[1, 1]) \cdot (a[1, 2]) \cdot (a[2, 2]) \cdot (a[2, 1]) + 5 \cdot (a[1, 1])^3 \cdot (a[1, 2]) + \\ &2 \cdot (a[1, 1])^2 \cdot (a[1, 2]) \cdot (a[2, 1]) + 5 \cdot (a[1, 1])^2 \cdot (a[1, 2]) \cdot (a[2, 2]) + \\ &(a[1, 1])^2 \cdot (a[1, 2]) \cdot (a[3, 1]) + (a[1, 1])^2 \cdot (a[1, 2]) + \\ &5 \cdot (a[1, 1])^2 \cdot (a[1, 3]) \cdot (a[3, 2]) + 10 \cdot (a[1, 1]) \cdot (a[1, 2])^2 \cdot (a[2, 1]) + \\ &10 \cdot (a[1, 1]) \cdot (a[1, 2]) \cdot (a[2, 1]) \cdot (a[1, 3]) \cdot (a[3, 1]) + \\ &4 \cdot (a[1, 1]) \cdot (a[1, 2]) \cdot (a[2, 1]) \cdot (a[2, 2]) + (a[2, 1]) \cdot (a[2, 2]) + \\ &(a[1, 1]) \cdot (a[1, 2]) \cdot (a[1, 3]) \cdot (a[3, 2]) + (a[2, 1]) \cdot (a[3, 2]) + \\ &2 \cdot (a[1, 1]) \cdot (a[1, 2]) \cdot (a[2, 1]) \cdot (a[2, 1]) + 5 \cdot (a[1, 1]) \cdot (a[1, 2]) \cdot (a[2, 2]) + \\ &(a[1, 1]) \cdot (a[1, 2]) \cdot (a[2, 2]) \cdot (a[2, 1]) + (a[2, 1]) \cdot (a[3, 1]) + \end{aligned}$$

21 R2:=add(cf(P,i)*A^i,i=0..4);

5+3·(a[[1, 1]])+6·(a[[3, 1]])+6·(a[[2, 1]])+
5·((a[[3, 1]])·(a[[1, 1]])+(a[[3, 3]])·(a[[3, 1]])+(a[[2, 1]])·(a[[3, 2]]))+
6·((a[[2, 1]])·(a[[1, 1]])+(a[[2, 3]])·(a[[3, 1]])+(a[[2, 2]])·(a[[2, 1]]))+
(a[[1, 1]])·(a[[2, 1]])·(a[[1, 1]])+(a[[2, 3]])·(a[[3, 1]])+(a[[2, 2]])·(a[[2, 1]]))+
(a[[3, 1]])·(a[[2, 1]])·(a[[1, 3]])+(a[[2, 3]])·(a[[3, 3]])+(a[[2, 2]])·(a[[2, 3]]))+
2·((a[[2, 1]])·(a[[2, 1]])·(a[[1, 2]])+(a[[2, 3]])·(a[[3, 2]])+(a[[2, 2]])²)+
(a[[3, 1]])·(a[[1, 3]])·(a[[1, 1]])+(a[[3, 3]])·(a[[1, 3]])+(a[[2, 3]])·(a[[1, 2]]))+
(a[[2, 1]])·(a[[1, 2]])·(a[[1, 1]])+(a[[3, 2]])·(a[[1, 3]])+(a[[2, 2]])·(a[[1, 2]]))+
(a[[1, 1]])·(a[[3, 1]])·(a[[1, 1]])+(a[[3, 3]])·(a[[3, 1]])+(a[[2, 1]])·(a[[3, 2]]))+
(a[[1, 1]])·(a[[3, 1]])·(a[[1, 3]])+(a[[2, 1]])·(a[[1, 2]])+(a[[1, 1]])²)+
(a[[3, 1]])·(a[[3, 1]])·(a[[1, 3]])+(a[[2, 3]])·(a[[3, 2]])+(a[[3, 3]])²)+
(a[[2, 1]])·(a[[3, 1]])·(a[[1, 2]])+(a[[3, 2]])·(a[[3, 3]])+(a[[2, 2]])·(a[[3, 2]]))+
(a[[3, 1]])·(a[[1, 1]])+(a[[3, 3]])·(a[[3, 1]])+(a[[2, 1]])·(a[[3, 2]]))·
(a[[1, 3]])·(a[[1, 1]])+(a[[3, 3]])·(a[[1, 3]])+(a[[2, 3]])·(a[[1, 2]]))+
(a[[2, 1]])·(a[[1, 1]])+(a[[2, 3]])·(a[[3, 1]])+(a[[2, 2]])·(a[[2, 1]]))·

22 normal(R2-R);

$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

23