Victor Rotger (UPC) : Weight one modular forms, Gross-Stark units and points on elliptic curves

Abstract : Let E be an elliptic curve over \mathbf{Q} and let ϱ_{\flat} and ϱ_{\sharp} be odd two-dimensional Artin representations such that $\varrho_{\flat} \otimes \varrho_{\sharp}$ is self-dual. The progress on modularity achieved in the last decades ensures the existence of normalised eigenforms f, g, h of respective weights 2, 1 and 1, giving rise to E, ϱ_{\flat} , and ϱ_{\sharp} via the constructions of Eichler-Shimura and Deligne-Serre. In this lecture I will discuss a conjecture by H. Darmon, A. Lauder and myself relating certain *p*-adic iterated integrals attached to the triple (f, g, h) to logarithms of Gross-Stark units in the number field cut out by $\mathrm{ad}^{0}(\varrho_{\flat})$ and global points on E defined over the number field cut out by $\varrho_{\flat} \otimes \varrho_{\sharp}$.