

## Notes on changes from Version 12 of SemigroupII to Version 13

Small changes in formatting, spelling corrections, and obvious minor typos will not be mentioned. I made no major changes, but I mention the other changes below. Some of these are questions of ascetics, in which case I am quite happy to do something else.

- 1) Page 3 (of Version 12) Definition 1.1: I moved the sentence “When ..  $\phi \in \Gamma$ ” to the line above the statement of the Definition. There was also a typo in this line which I fixed: “ $\phi_1$ ” should be  $\phi_i$ . I thought it was better to keep the definition as short as possible, but if you want to move the sentence back into the definition, this is fine with me.
- 2) page 3, line -10:  $\lambda_i$  is changed to  $\lambda_{i-1}$ .
- 3) Page 4: In the proof of Lemma 1.2, I changed all  $\lambda_i$  to  $\tau_i$ , as we just defined  $\lambda_i$  to be a projection map.
- 4) On page 4: before Theorem 1.1, and on Page 5 before Theorem 1.3 we have almost the exact same sentences defining  $p_2 \subset p_1 \subset p_0$  and the  $e_{m_i}$ . I did not change anything. Probably better to repeat than have people not able to figure out our notation.
- 5) On Page 5: line 10: I changed “ $y \in \mathbf{N}$ ” to  $y \in \mathbf{Z}_+$ ” because there is a little trouble in the bound when  $y = 0$ , as  $0^0$  is an indeterminate form. Of course  $\mathbf{N}$  is the natural place to start, but we probably should address the fact that the bound is a little different in this case if we want to use  $\mathbf{N}$ .
- 6) First 1/2 of page 5: You commented that we can use Neumann here, as I understand it to conclude that  $T$  is well ordered? I think that well ordering follows from much more elementary considerations in this case than quoting Neumann. Our set  $U$  has 1 as its minimum element, and there are only finitely many elements of  $U$  which are less than or equal to any positive integer  $n$ . Thus for any  $n \in \mathbf{N}$ , the set  $mU \cap [0, n[$  is the empty set for  $m > n$ . Since for each  $m \in \mathbf{N}$ , the set  $mU \cap [0, n[$  is a finite set, we have that  $T \cap [0, n[$  must be a finite set. This is enough to conclude that  $T$  is well ordered. Have I missed some subtle (or maybe not so subtle) point?
- 7) page 7: In the statement of Corollary 1.6, I removed “from the Lemma”, so that it now reads “we deduce that when”. The corollary is stated as a corollary to Theorem 1.3.
- 8) Page 7, Statement of Theorem 1.7: I did not change anything here. With the notation introduced in the previous paragraph it is OK. I have mixed feelings about this nota-

tion, as the interval would not be correct when  $p_i = p_{i+1}$ , except that we have defined it to be something other than what it appears to be in this case. On the other hand, if we use notation to distinguish the 2 cases we have to go to a more cumbersome statement of the theorem, such as the one that I sent to you. Certainly the theorem looks a lot nicer the way you stated it.

- 9) Page 8, line 13: I changed the definition of  $s_1(\epsilon_1, \phi_2)$  to reflect the fact that we have to keep track of the whole history of  $\phi$ .
- 10) Page 8, line 15: I changed the inequality to an equality on this line. It does not affect the final statement, but this is the actual statement of Theorem 1.3 b).
- 11) Page 8, after line 15: I added “and define  $s_1(\epsilon_1, y_2) = 1$ ”. Evidently  $s_1$  could be anything here, but we are expected to produce some kind of  $s_1$  to finish the statement of the theorem.
- 12) page 14, lines 18 and 19: I changed the  $\phi_i$  to  $\eta_i$ .
- 13) Page 15, line 14 - 15: The statement “One can check ..  $+v(P_{i-1})$ ”, seems not to fit (we are working with  $Q_i$ , not  $P_i$ ). I removed it since the information which is recorded here is stated a few lines later, in notation appropriate for this result. I do not think that this information is needed until it is stated, but there could be a reason for stating these formulas here, at an earlier place
- 14) page 17 line 13: In this sentence the  $\alpha$ s and  $\beta$ s need to be interchanged, to reflect the fact that the role of  $\alpha$  and  $\beta$  has been changed in the rest of the proof.