(New) Challenges in Random Number Generation for Cryptography

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Workshop on Randomness and Arithmetics for Cryptography on Hardware, April 2019



Basic RNG classes

Deterministic (Pseudo-) random number generators (PRNG)

- Algorithmic generators
- Usually faster, with good statistical properties
- Must be computationally secure, i. e. it should be computationally difficult to guess the next or previous values
- Physical (True-) random number generators (TRNG)
 - Using some physical source of randomness
 - Unpredictable, usually having suboptimal statistical characteristics
 - Usually slower
- Hybrid random number generators (HRNG)
 - Deterministic RNG seeded repeatedly by a physical random number generator
 - True RNG with algorithmic (e. g. cryptographic) postprocessing



RNGs in logic devices

► RNGs – usually a part of a Cryptographic SoC ⇒ in logic devices

- Logic devices (ASICs or FPGAs)
 - Aimed at implementation of deterministic systems
 - Designed so that the deterministic behavior dominates
 - Some analog blocks are sometimes available (PLL, RC-oscillator, A/D and D/A converters, etc.)

Challenge #1

Implementation of PRNGs in logic devices is straightforward ... but ...

... finding and exploiting correctly a robust physical source of randomness needed in TRNGs is a challenging task



Classical versus modern TRNG design approach

- Two main security requirements on RNGs:
 - R1: Good statistical properties of the output bitstream
 - R2: Output unpredictability
- Classical approach:
 - Assess both requirements using statistical tests difficult
- Modern ways of assessing security:
 - Evaluate statistical parameters using statistical tests
 - Evaluate entropy using entropy estimator (stochastic model)
 - Test online the source of entropy using dedicated statistical tests

Objective of the talk

To show on practical examples

- Why the thorough security assessment is so important
- What are remaining challenges in TRNG design and evaluation

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Fair tossing of fair coins - considered as an ideal TRNG 1/2



How much entropy per trial, if ten coins are used?



Fair tossing of fair coins - considered as an ideal TRNG 202



- What can be the frequency of trials?
- Can you get 100 random bits per second, when using just ten coins?



Tossing (partially) unfair coins - realistic TRNG



How much entropy per trial, if:

- One (independent) fair coin
- Four correlated coins
- Two biased coins
- Three manipulable coins
- Can the output be manipulable, if the ten coins values are bit-wise XORed in order to get one output bit?



Tossing (partially) unfair coins - realistic TRNG

In the context of oscillator based TRNG:



How much entropy per trial, if:

- One (independent) fair coin
- Four correlated coins
- Two biased coins
- Three manipulable coins
- Can the output be manipulable, if the ten coins values are bit-wise XORed in order to get one output bit?



Conclusions regarding our study case

- Design of a RNG is rather a physical than a mathematical project
- The physical parameters of the source of randomness must be thoroughly evaluated:
 - Distribution of random values (bias)
 - Correlation
 - Dependence (if many sources)
 - Manipulability
 - Agility (spectrum)



Outline

Contemporary TRNG design challenges

- Sources of randomness and entropy extraction methods
- Stochastic models and entropy estimators
- Postprocessing methods
- Statistical tests objectives and strategies
- Security evaluation of RNGs in a certification process
 - Main approaches in RNG security certification
 - European AIS20/31 vs American NIST SP800-90





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Contemporary TRNG design



- Source of the digital noise
 - Should give as much entropy per bit as possible
 - Should enable sufficient bit-rate
 - Shouldn't be manipulable (robustness)
- Postprocessing
 - Algorithmic enhances statistics without reducing the entropy
 - Cryptographic for unpredictability when source of entropy fails
- Embedded tests
 - Fast total failure test with low probability of false alarms





Sources of randomness in logic devices

- Commonly used sources related to some physical process, basically coming from electric noises
 - Clock jitter: short-term variation of an event from its ideal position
 - Oscillatory metastability: ability of a bi-stable circuit (e.g. an RS flip-flop) to oscillate for an indefinite period
 - **Metastability**: ability of an unstable equilibrium electronic state to persist for an indefinite period in a digital system (rare)
 - **Initialization of flip-flops**: initialization of a flip-flop (or a memory element) to a random state (after power-up or periodically)
 - Chaos: stochastic behavior of a deterministic system which exhibits sensitive dependence on initial conditions (needs analog blocks)



Sources of randomness: jittered clock signals

- Clock jitter the most frequently used in logic devices
- The jitter in clock generators is caused by ¹
 - Local noise sources
 - Global noise sources



Sources in red are manipulable!

Challenge #2

Entropy should be estimated using only local non-manipulable uncorrelated sources (e.g. thermal noise)

^I B. Valtchanov, A. Aubert, F. Bernard, and V. Fischer, Modeling and observing the jitter in ring oscillators implemented in FPGAs, DDECS 2008

Clock generators: Ring oscillators (ROs) 1/3

- Ring oscillators single event oscillators ¹
 - One event (rising and falling edge) is propagated in the ring
 - Half period: sum of delays of individual ring elements
 - The most common free running oscillators in logic devices easy to implement
 - Clock frequency easy to manipulate (temperature, power voltage) but not the jitter coming from the thermal noise

ena
$$U_1(t)$$
 U_2 U_2 U_n

Challenge #3

The clock jitter is caused by thermal noises but also by correlated low frequency noises, while the second tend to dominate

¹ V. Fischer, P. Haddad, and A. Cherkaoui, Ring Oscillators ans Self-Timed Rings in True Random Number Generators, in N. Yoshifumi (ed): Oscillator Circuits: Frontiers in Design, Analysis and Applications, IET 2016



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Clock generators: Transition effect ring oscillators (TEROs) 2/3

- Two-event oscillators with collisions ¹
 - Easy to implement in logic devices
 - Two events (edges) are propagated in the ring until one reaches the second
 - Easy to convert to random numbers (number of periods)



Challenge #4

Increase repeatability – number of periods (and thus entropy) differs significantly device by device

¹ V. Fischer, P. Haddad, and A. Cherkaoui, Ring Oscillators ans Self-Timed Rings in True Random Number Generators, in N. Yoshifumi (ed): Oscillator Circuits: Frontiers in Design, Analysis and Applications, IET 2016

Clock generators: Self-timed rings (STRs) 33

- Multi-event oscillators without collisions¹
 - Using Muller cells relatively easy to implement in logic devices
 - Several events (edges) are propagated in the ring asynchronous logic avoids collisions
 - Frequency does not depend on number of ring elements



Challenge #5

Ensure the evenly-spaced mode (i.e. avoid the burst mode) to guarantee entropy

¹ V. Fischer, P. Haddad, and A. Cherkaoui, Ring Oscillators ans Self-Timed Rings in True Random Number Generators, in N. Yoshifumi (ed): Oscillator Circuits: Frontiers in Design, Analysis and Applications, IET 2016

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Converting analog noises to a raw binary signal 113

- To eliminate global manipulable jitter sources, two identical free-running oscillators are used
- We compared two ways of randomness extraction ¹
 - Sampling the jittered clock signal
 - Counting periods of the jittered clock signal



Sampler based randomness extraction

Counter based randomness extraction



Entropy Estimates from the 8-th order Markov chain model

Randomness extraction method: sampling the jittery clock

Jitter accumulation time	Markov	AIS 31	AIS 31 T8	NIST	NIST
	chain	Procedure B		800-90B	800-90B
Periods of s ₂	min-entropy		Shannon entropy	IID	min-entropy
10 000	0.8102	failed	0.9844	non-IID	0.648
20 000	0.8105	failed	0.9851	non-IID	0.647
30 000	0.8102	failed	0.9847	non-IID	0.648
50 000	0.9369	failed	0.9992	non-IID	0.673
100 000	0.9012	failed	0.9935	non-IID	0.670

Randomness extraction method: counting the jittery clock periods

Jitter accumulation time	Markov chain	AIS 31	AIS 31 T8	NIST	NIST
		Procedure B		800-90B	800-90B
Periods of s ₂	min-entropy		Shannon entropy	IID	min-entropy
10 000	0.8089	failed	0.9966	non-IID	0.844
15 000	0.9769	passed	0.9998	non-IID	0.931
20 000	0.9865	passed	0.9999	IID	0.999
25 000	0.9907	passed	0.9999	IID	0.998
100 000	0.9910	passed	0.9999	IID	0.998

Conclusions regarding the digital noise source

- The source of randomness must be clearly defined, well characterized and quantified
- With respect to the entropy harvesting method, it should serve as an input parameter of the stochastic model
- The entropy harvesting method (digitization) must be as efficient as possible – the method using counter gives much better results
- Entropy should be estimated using a stochastic model it cannot be measured



Stochastic models – objectives

- Stochastic model definition:
 - Stochastic model specifies a family of probability distributions that contains all possible distributions of the raw-random numbers
- Main objectives characterize:
 - Probability of ones: Pr(X = 1)
 - Probability of an n-bit vector: $Pr(X_1 = x_1, X_2 = x_2, ..., X_n = x_n)$
 - ... and from them the entropy
- Two kinds of entropy can be evaluated:
 - Entropy if exploited random variables are IID
 - Conditional entropy if exploited random variables are non-IID

Challenge #7

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 Propose a TRNG stochastic model based on some measurable parameters

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TRNG Design Challenges RNG security evaluation Conclusions

Comprehensive example of a stochastic model

- Model of a free-running oscillators based elementary TRNG¹
- The lower bound of the Shanon entropy rate per bit at the generator output is given as:

$$H_{min} \approx 1 - \frac{4}{\pi^2 \ln(2)} e^{-4\pi^2 Q} = 1 - \frac{4}{\pi^2 \ln(2)} e^{-\frac{4\pi^2 \sigma_{fit}^2 T_2}{T_1^3}}$$
 (1)

The lower entropy bound is determined by measurable parameters!

- Mean frequencies of the two ring oscillators
- Jitter variance per period T₁
- These measurements together with the model will constitute a basis for dedicated tests!



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¹ M. Baudet *et al.*, On the security of oscillator-based random number generators. Journal of Cryptology, 2011.

Normal variance vs Allan variance 1/3

Normal variance - unbounded in the presence of low-frequency noises

Estimate of the normal variance:

$$\sigma_y^2 = E(y^2) - E^2(y).$$

(2)

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Allan variance - an average fractional frequency can be used

- Average frequency deviation \overline{y}_k over a time interval of length τ
 - $\bullet\,$ Corresponds to the fluctuations while counting the number of periods of the jittery signal over τ
- Estimate of the Allan variance:

$$\sigma_{y}^{2}(\tau) = \frac{1}{2(M-1)} \sum_{i=1}^{M-1} (\overline{y}_{i+1} - \overline{y}_{i})^{2}.$$
 (3)

 \hookrightarrow *M* : total number of \overline{y}_k 's.

For α = 0, σ_y²(τ) is an unbiased estimator of the variance even for a finite M

Normal variance vs Allan variance 23

Hardware implementations

Statistical variance



3 adders/subtractors, 2 multipliers

Allan variance



1 adder/subtractor, 1 multiplier

Comparison with the state-of-the-art methods

Method	Area	1	f _{max}	Power	
	ALM/Regs	DSPs	[MHz]	[mW]	
Haddad et al. (DATE14)	119/160	2	178.3	6-7	
Fischer and Lubicz (CHES14)	169/200	4	187.7	7-8	
Allan variance based method (CHES18)	49/117	1	238.5	4-5	

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Normal variance vs Allan variance 3/3



- Variance dependence on the number of samples M
 - Allan variance stable
 - Normal variance increases with *M*



- Variance dependence on accumulation period k
 - Allan variance always below statistical variance
 - Normal variance causes entropy overestimation
- Similar results for both types of free running oscillators studied¹



¹E. N. Allini *et al.*, Evaluation and monitoring of free running oscillators serving as source of randomness. CHES, 2018.

Postprocessing of the raw random signal

- Should make obtained numbers statistically and computationally indistinguishable from the output of an ideal TRNG
- The generated values can be
 - Biased (or not uniformly distributed)
 - Correlated
 - Entropy rate can be insufficient
- Main security objectives
 - Enhance above-mentioned statistical parameters
 - Internal memory of the postprocessing algorithm should maintain some entropy, before the total failure test will trigger alarm
 - Cryptographic postprocessing should ensure unpredictability (if the entropy source fails)

Challenge #8

Obtain a high quality raw random signal so that the post-processing is not needed!

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Statistical tests – objectives and strategies

- Statistical testing of the generator is necessary, but not sufficient it cannot substitute
 - it cannot substitute
 - Cryptanalysis in the case of DRNGs
 - Analysis of the entropy rate in the case of the TRNGs
- Two phases of testing
 - **Off-line testing** (preliminary) during the design and security validation process (by developers and evaluators)
 - Using testing procedures required by security standards
 - Using general purpose (black box) statistical tests (optional)
 - On-line testing (operational) testing when in use in a cryptographic application (testing by the application itself) usually using dedicated tests
 - Startup test(s)
 - Continuous test(s)
 - On-demand test(s)



Dedicated (white box) statistical tests 1/3

- Adapted to the generator's principle, more efficient in evaluation of its weaknesses
- Preferably based on the generator's statistical model
- One or more dedicated tests can constitute a basis of embedded tests
- At least the continuous test (the total failure test) should be a white box test adapted to the generator's principle

Challenge #9

Propose efficient dedicated tests based on the stochastic model

Challenge #10

Verify and demonstrate efficiency of the tests

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Dedicated (white box) statistical tests 2/3

Total failure test (Continuous test)

- The total failure of the entropy means that the entropy rate at the generator's output has fallen to 0
- This catastrophic scenario must be detected very fast and no further data can be output once detected
- Triggering the total failure alarm has another important consequence: the generator must be reseted and the (long) startup procedure must be executed – probability of false alarms must be very small
- The speed and the robustness of the test can be more easily ensured if the testing point is closer to the source of randomness
- The larger latency of the test is allowed only if the numbers are buffered (e.g. in a FIFO)

Dedicated (white box) statistical tests 3/3

Online tests

- Online tests should detect intolerable weaknesses
- What means an intolerable weakness should be defined according to the generator's principle, e.g. from the model
- Online tests can be performed
 - Regularly
 - On demand
 - After an event (e.g. self-test of the cryptographic module)
 - Continuously (preferable, but expensive power consumption)
- Once the online test alarm is triggered, the generator output must be stopped
- During the time interval between the randomness failure and the alarm, the generator must behave as a DRNG



Dedicated tests suitable for oscillator based TRNG

Recall

- The stochastic model of our oscillator based TRNG depends on
 - Variance of the jitter (σ^2)
 - Periods T_1 and T_2 and their relationship

Solution

The Online tests should measure the jitter variance and periods T₁ and T₂

Problem

But how can the generator totally fail?



Mutual dependence of ring oscillator frequencies





Testing conditions

- Two similar ROs are implemented inside the device
- Frequencies are measured outside the device
- The power supply varies between 1.0 and 1.2 V

Results

 Frequencies approach and lock to the same value during some voltage interval.

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¹U. Mureddu *et al.*, Experimental Study of Locking Phenomena on Oscillating Rings Implemented in Logic Devices.⁴

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TRNG Design Challenges RNG security evaluation Conclusions

Randomness Models Postprocessing Testing

Oscillator based TRNG including dedicated tests

- Online test is based on the Allan variance evaluation
- Total failure test evaluates repetitions of counter values
 - Extremely efficient to detect locking
 - Extremely fast latency few random bits



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Security evaluation of RNGs in a certification process

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3 Conclusions



Main approaches in RNG security certification

- Approach of the German BSI (Federal Office for Information Security) – de facto standard in Europe
 - AIS 20 / AIS 31 A proposal for functionality classes for random number generators, v. 1.0 (2001) and 2.0 (2011)
- Approach of the American NIST (National Institute for Standards and Technology)
 - **NIST SP 800-90A** Recommendation for Random Number Generation Using Deterministic Random Bit Generators (2012)
 - **NIST SP 800-90B** Recommendation for the Entropy Sources Used for Random Bit Generation (2018)
 - NIST SP 800-90C Recommendation for Random Bit Generator (RBG) Constructions (draft from 2012)



Example of a high end AIS 20 / AIS 31 PTRNG class

PTG.3



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Dedicated tests & entropy

- Total failure, online and startup test requirements as in PTG.2
- Shanon entropy of internal random numbers > 0,997
- Cryptographic post-proc. must be tested by a KAT

Evaluation procedures

 Depending on availability and quality of the raw binary signal: Method A (preferable) or Method B

 Highest security – the information-theoretical security combined with the computational security

Comparison of the European and American approaches 113





Naming

- Digital noise source
- Algorithmic & cryptographic post-processing
- Digital noise source + Post-processing => Internal random numbers
- Tot test and on-line tests

Naming

- Digital noise source
- Entropy conditioner (entropy extractor)
- Digital noise + Entropy conditioner + Health test => Entropy source

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Health tests

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Comparison of the European and American approaches 213

Embedded tests

Tot test

- Fast and low false alarm probability
- Test not specified

On-line tests

Detect non tolerable weaknesses

Entropy estimation using a model

Stochastic model must be given

- For IID sources:
 Shannon entropy is computed
- For non-IID sources:
 Conditional entropy is computed

Health tests

Continuous tests (min. 2 required)

- Repetition count test
- Adaptive proportion test

On-demand tests

Test not specified

Entropy estimation using tests

For claimed IID sources

- Verification if IID
 - 11 + 5 tests
- Min-entropy estimation for IID

For non-IID sources

Min-entropy estimation for non-IID

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I0 statistical tests

Restart test

One sanity check

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Comparison of the European and American approaches 33

Testing by security evaluator

- Depending on the TRNG class, Procedure A and B is applied.
- For PTG.2 and PTG.3, the RAW binary signal must be available outside the TRNG (Procedure B).

Testing by security evaluator

 The RAW binary signal does not need to be available outside the TRNG (only inside for the health test)

Conclusion

More stringent approach, but more risky: bad model means bad entropy estimation and possibly bad dedicated test, which means weak generator. Unfortunately, the model construction and verification is not straightforward.

Conclusion

Solution simpler for the designer, but entropy evaluation might not be precise: we obtain the solution that is somehow less risky, but also less precise (for non-IID sources, the entropy can be underestimated).

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TRNG Design Challenges RNG security evaluation Conclusions

Towards compatibility with both European and American approach and high security requirements of French DGA 1/2

- Dedicated tests verify operation of the source of the digital noise
- NIST tests test operation of the source, FIFO and S2P converter
- KAT test verifies integrity of the DRNG



TRNG Design Challenges RNG security evaluation Conclusions

Towards compatibility with both European and American approach and high security requirements of French DGA 212

- Source of randomness is modeled separately
- **NIST tests** and **KAT test** guarantee integrity of the entire TRNG



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Conclusions

- Designing robust generators giving high-quality true random numbers in logic devices remains a challenge
- Testing the source of randomness before entropy extraction increases precision and speed of the tests and thus security
- We have shown that the whole TRNG data path must be tested to ensure security
- Efficiency of all embedded tests must be verified

Last but not least ...

We have confirmed these statements by many practical results published in proceedings of high-end conferences and in scientific papers



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