

nom	diagramme	degrés	codegrés	orbites	corps	$ ZG $	\mathbf{z}	#cl.	G/ZG	
$G(de, e, r)$ $e, d \geq 2$		$ed[1..r-1]$ rd	$ed[0..r-1]$	$s:r, t:der(r-1)/2$ except $r=2, e$ even $s:2, t_2:de/2, t'_2:de/2$	$\mathbb{Q}(\zeta_{de})$	$d(e \wedge r)$	$s^{\frac{r}{e \wedge r}} (t'_2 t_2 t_3 \dots t_r)^{\frac{e(r-1)}{e \wedge r}}$			
G_{15}		$tus = stu$ $ustut = stutu$	12, 24	0, 24	$s6, t12, u8$	$\mathbb{Q}(\zeta_{24})$	12	$ustut$	42	\mathfrak{S}_4
A_r		$[2..r, r+1]$	$[0..r-1]$	$t: \frac{r(r+1)}{2}$	\mathbb{Q}	1	$(t_1 \dots t_r)^{r+1}$			
G_4		4, 6	0, 2	$s4$	$\mathbb{Q}(\zeta_3)$	2	$(st)^3$	7	\mathfrak{A}_4	
G_8		8, 12	0, 4	$s6$	$\mathbb{Q}(i)$	4	$(st)^3$	16	\mathfrak{S}_4	
G_{16}		20, 30	0, 10	$s12$	$\mathbb{Q}(\zeta_5)$	10	$(st)^3$	45	\mathfrak{A}_5	
G_{25}		6, 9, 12	0, 3, 6	$s12$	$\mathbb{Q}(\zeta_3)$	3	$(stu)^4$	24	$3^2 \rtimes SL_2(3)$	
G_{32}		12, 18, 24, 30	0, 6, 12, 18	$s40$	$\mathbb{Q}(\zeta_3)$	6	$(stuv)^5$	102	$PSp_4(3)$	
$G(d, 1, r)$ $d \geq 2$		$d[1..r]$	$d[0..r-1]$	$s:r$ $t: \frac{dr(r-1)}{2}$	$\mathbb{Q}(\zeta_d)$	d	$(st_2 t_3 \dots t_r)^r$			
G_5		6, 12	0, 6	$s4, t4$	$\mathbb{Q}(\zeta_3)$	6	$(st)^2$	21	\mathfrak{A}_4	
G_{10}		12, 24	0, 12	$s8, t6$	$\mathbb{Q}(\zeta_{12})$	12	$(st)^2$	48	\mathfrak{S}_4	
G_{18}		30, 60	0, 30	$s20, t12$	$\mathbb{Q}(\zeta_{15})$	30	$(st)^2$	135	\mathfrak{A}_5	
G_{26}		6, 12, 18	0, 6, 12	$s9, t12$	$\mathbb{Q}(\zeta_3)$	6	$(stu)^3$	48	$3^2 \rtimes SL_2(3)$	

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$G(2d, 2, r)$ $d \geq 2$		$2d[1 \dots r - 1]$ rd	$2d[0 \dots r - 1]$	$s:r, t:r(r-1)d$ except $r=2:$ $s:2, t_2:d, t'_2:d$	$\mathbb{Q}(\zeta_{2d})$	$d(2 \wedge r)$	$s^{\frac{r}{2 \wedge r}} (t'_2 t_2 t_3 \dots t_r)^{\frac{2r-2}{2 \wedge r}}$		
G_7		12, 12	0, 12	$s6, t4, u4$	$\mathbb{Q}(\zeta_{12})$	12	stu	42	\mathfrak{A}_4
G_{11}		24, 24	0, 24	$s12, t8, u6$	$\mathbb{Q}(\zeta_{24})$	24	stu	96	\mathfrak{S}_4
G_{19}		60, 60	0, 60	$s30, t20, u12$	$\mathbb{Q}(\zeta_{60})$	60	stu	270	\mathfrak{A}_5
$G(e, e, r)$ $e \geq 2, r > 2$		$e[1 \dots r - 1]$ r	$e[0 \dots r - 2]$ $(r - 1)e - r$	$t_2 : \frac{er(r-1)}{2}$	$\mathbb{Q}(\zeta_e)$	$e \wedge r$	$(t'_2 t_2 t_3 \dots t_r)^{\frac{e(r-1)}{e \wedge r}}$		
$G(e, e, 2) = I_2(e)$ $e \geq 3$		2, e	0, $e - 2$	e odd $s:e$ else $s:e/2, t:e/2$	$\mathbb{Q}(\zeta_e + \zeta_e^{-1})$	$e \wedge 2$	$(st)^{e/(e \wedge 2)}$	e odd: $(e+3)/2$ else $(e+6)/2$	
G_6		4, 12	0, 8	$s6, t4$	$\mathbb{Q}(\zeta_{12})$	4	$(st)^3$	14	\mathfrak{A}_4
G_9		8, 24	0, 16	$s12, t6$	$\mathbb{Q}(\zeta_8)$	8	$(st)^3$	32	\mathfrak{S}_4
G_{17}		20, 60	0, 40	$s30, t12$	$\mathbb{Q}(\zeta_{20})$	20	$(st)^3$	90	\mathfrak{A}_5
G_{14}		6, 24	0, 18	$s12, t8$	$\mathbb{Q}(\zeta_3, \sqrt{-2})$	6	$(st)^4$	24	\mathfrak{S}_4
G_{20}		12, 30	0, 18	$s20$	$\mathbb{Q}(\zeta_3, \sqrt{5})$	6	$(st)^5$	27	\mathfrak{A}_5
G_{21}		12, 60	0, 48	$s30, t20$	$\mathbb{Q}(\zeta_{12}, \sqrt{5})$	12	$(st)^5$	54	\mathfrak{A}_5

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G_{12}		6, 8	0, 10	s_{12}	$\mathbb{Q}(\sqrt{-2})$	2	$(stu)^4$	8	\mathfrak{S}_4	
G_{13}		8, 12	0, 16	s_6, tu_{12}	$\mathbb{Q}(\zeta_8)$	4	$(stu)^3$	16	\mathfrak{S}_4	
G_{22}		12, 20	0, 28	s_{30}	$\mathbb{Q}(i, \sqrt{5})$	4	$(stu)^5$	18	\mathfrak{A}_5	
$G_{23} = H_3$		2, 6, 10	0, 4, 8	s_{15}	$\mathbb{Q}(\sqrt{5})$	2	$(stu)^5$	10	\mathfrak{A}_5	
G_{24}		$tu(stu)^2s = utu(stu)^2$	4, 6, 14	0, 8, 10	s_{21}	$\mathbb{Q}(\sqrt{-7})$	2	$(stu)^7$	12	$GL_3(2)$
G_{27}		$tu(stu)^3t = utu(stu)^3$	6, 12, 30	0, 18, 24	s_{45}	$\mathbb{Q}(\zeta_3, \sqrt{5})$	6	$(uts)^5$	34	\mathfrak{A}_6
$G_{28} = F_4$		2, 6, 8, 12	0, 4, 6, 10	s_{12}, t_{12}	\mathbb{Q}	2	$(stuv)^6$	25	$2^4 \rtimes (\mathfrak{S}_3 \times \mathfrak{S}_3)$	
G_{29}		4, 8, 12, 20	0, 8, 12, 16	s_{40}	$\mathbb{Q}(i)$	4	$(stvu)^5$	37	$2^4 \rtimes \mathfrak{S}_5$	
$G_{30} = H_4$		2, 12, 20, 30	0, 10, 18, 28	s_{60}	$\mathbb{Q}(\sqrt{5})$	2	$(stuv)^{15}$	34	$(\mathfrak{A}_5 \times \mathfrak{A}_5) \rtimes 2$	

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G_{31}		8, 12, 20, 24	0, 12, 16, 28	s_{60}	$\mathbb{Q}(i)$	4	$(stuvw)^6$	59	$2^4 \rtimes \mathfrak{S}_6$
G_{33}		4, 6, 10, 12, 18	0, 6, 8, 12, 14	s_{45}	$\mathbb{Q}(\zeta_3)$	2	$(stuvw)^9$	40	$SO_5(3)'$
G_{34}		6, 12, 18, 24, 30, 42	0, 12, 18, 24, 30, 36	s_{126}	$\mathbb{Q}(\zeta_3)$	6	$(stuvw x)^7$	169	$PSO_6^-(3)'.2$
$G_{35} = E_6$		2, 5, 6, 8, 9, 12	0, 3, 4, 6, 7, 10	s_{36}	\mathbb{Q}	1	$(s_1 \dots s_6)^{12}$	25	$SO_6^-(2)'$
$G_{36} = E_7$		2, 6, 8, 10, 12, 14, 18	0, 4, 6, 8, 10, 12, 16	s_{63}	\mathbb{Q}	2	$(s_1 \dots s_7)^9$	60	$SO_7(2)$
$G_{37} = E_8$		2, 8, 12, 14, 18, 20, 24, 30	0, 6, 10, 12, 16, 18, 22, 28	s_{120}	\mathbb{Q}	2	$(s_1 \dots s_8)^{15}$	112	$SO_8^+(2)$