

In the proof of items (1) and (2) in Proposition 2.6 of [MP21] we refer twice to Lemma 2.5 which only applies in the compact case. Adopting the notation introduced therein, it can be replaced by the following:

**Lemma.** *Let  $X$  be a cohomologically Stein  $k$ -analytic space,  $M$  a finitely generated  $\mathcal{O}_X(X)$ -module and  $\tilde{M}$  the associated coherent sheaf on  $X$ . Then, the natural map  $M \rightarrow \tilde{M}(X)$  is surjective.*

*Proof.* Let  $m_1, \dots, m_n$  be a set of generators of  $M$ . The morphism of coherent sheaves  $\varphi: \mathcal{O}_X^n \rightarrow \tilde{M}$ ,  $(f_1, \dots, f_n) \mapsto f_1 m_1 + \dots + f_n m_n$  is surjective by construction of  $\tilde{M}$ . The short exact sequence of coherent sheaves  $0 \rightarrow K \rightarrow \mathcal{O}_X^n \rightarrow \tilde{M} \rightarrow 0$  on  $X$ , where  $K = \text{Ker } \varphi$ , induces a short sequence of  $\mathcal{O}_X(X)$ -modules

$$0 \longrightarrow K(X) \longrightarrow \mathcal{O}_X(X)^n \longrightarrow \tilde{M}(X) \longrightarrow 0$$

because  $H^1(X, K) = 0$  by the cohomologically Stein hypothesis. It follows that  $m_1, \dots, m_n$  generate  $\tilde{M}(X)$  as an  $\mathcal{O}_X(X)$ -module.  $\square$

#### REFERENCES

- [MP21] M. Maculan and J. Poineau, *Notions of Stein spaces in non-Archimedean geometry*, J. Algebraic Geom. **30** (2021), 287–330.